

# Dynamic Modes Maps of Incommensurate Superstructures with Elementary Cell Multiplication



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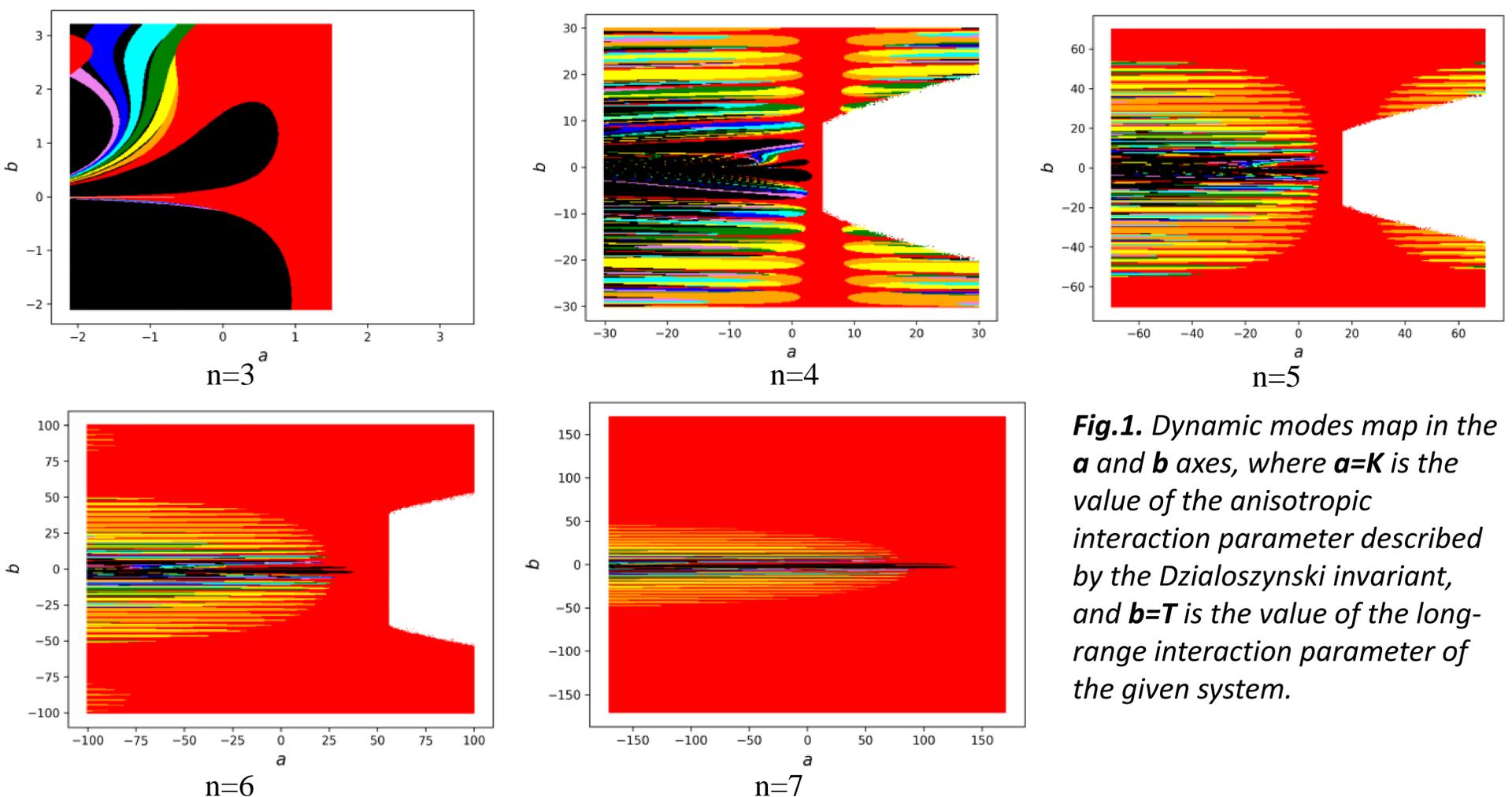
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## Introduction

The crystals of the  $[N(CH_3)_4]_2MeCl_4$  group (where  $Me = Zn, Cu, Co, Fe$ ) are characterized by a complex sequence of phase transitions, including the transition to the incommensurate phase with nano-periodicity (with a period of  $\sim 100\div 160$  nm). At lower temperatures (i.e., with an increase in anisotropic interaction), the incommensurate superstructure is characterized by a change in its mode from sinusoidal to soliton with a transition to the stochastic mode and the appearance of a chaotic phase. The emerging incommensurate superstructure is characterized by modulation of spontaneous polarization and spontaneous deformation or their sequence. Such a large number of commensurate (long-periodic phases) and sequences of incommensurate phases in these objects stimulated the research of dynamic regime maps of these systems.

## Results and Discussion

Creating a dynamic modes map is one of the most visual ways to qualitatively assess a system's behavior. Figure shows the maps of dynamic modes for systems characterized by different multiplication of the elementary cell.



**Fig.1.** Dynamic modes map in the  $a$  and  $b$  axes, where  $a=K$  is the value of the anisotropic interaction parameter described by the Dzialoszynski invariant, and  $b=T$  is the value of the long-range interaction parameter of the given system.

In our case, the two-dimensional mappings were defined by recurrence equations as follows:  $x_{n+1}=f(x_n, y_n)$ ;  $y_{n+1}=g(x_n, y_n)$ . A function describing the amplitude ( $R$ ) of the incommensurability wave or its change ( $R'$ ) was used as a function  $f(x_n, y_n)$ . The function  $g(x_n, y_n)$  acted as a function describing the phase ( $\phi$ ) of the incommensurability wave or its change ( $\phi'$ ). For this system, the Lyapunov exponents characterized by the most significant changes are described by spatial changes in the order parameter's amplitude ( $R'$ ) and phase ( $\phi'$ ). Therefore, Figure 1 shows a two-dimensional mapping, where  $R'$  and  $\phi'$  were used as functions  $f()$  and  $g()$ , respectively.

## Conclusion

The obtained maps of dynamic modes are characterized by an increase in the number of periodicities, with an increase in the multiplication value of the elementary cell. At  $n=3$ , when  $K$  and  $T$  change ( $K, T=0\div 1$ ), the existence of two disproportionately modulated phases is traced, which is observed in  $[N(CH_3)_4]_2CuCl_4$  crystals. Applying an external field (mechanical or electrical stress) expanded the range of periodicities.